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Claims

What is claimed is:

1. A method for encrypting a message to be transmitted over a network, wherein the method comprises the steps of:

encrypting the message for transmission over the network, the resulting encrypted message having associated therewith a proof of correctness indicating that the message is of a type that allows decryption by one or more escrow authorities; and

transmitting the encrypted message through the network to a recipient, wherein in traversing the network the proof of correctness associated with the encrypted message is checked by at least one module of a server of the network.

- 2. The method of claim 1 wherein the encrypted message is generated by first selecting a random element k from an interval $[0 \dots q-1]$, where q denotes the size of a group G, using modulo p, then computing a symmetric key $K = \text{hash}(g^k \mod p)$ for a symmetric encryption technique (E, D), where g is a generator of the group G, and finally computing the encrypted message in the form of a ciphertext $M' = E_K(M)$, where M denotes the message being encrypted.
- 3. The method of claim 1 wherein also associated with the encrypted message is an element $a = y_d^{\alpha} * g^k$ and an element $b = g^{\alpha}$, where α is chosen uniformly at random from $[0 \dots q-1]$ and y_d is a public encryption key.
- 4. The method of claim 3 wherein the proof of correctness comprises a proof of knowledge of (α, k) that does not reveal y_d^{α} or g^k .
- 5. The method of claim 1 wherein also associated with the encrypted message is a certificate C_d on a public encryption key y_d .
- 6. The method of claim 5 wherein the encrypted message is considered valid by the module of the server if the proof of correctness is valid and the certificate C_d is valid.

- 7. The method of claim 6 wherein the certificate C_d is considered valid if it is a valid certificate for encryption.
- 8. The method of claim 1 wherein the proof of correctness comprises a proof c in the form 5 of a triple (r, s1, s2).
 - 9. The method of claim 8 wherein the proof c is generated using the steps of:

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selecting two elements \beta 1 and \beta 2 at random from an interval [0 \dots q-1];
computing r = y_d^{\beta 2} g^{\beta 2} \pmod{p};
computing e = hash(r, a);
computing s1 = \beta 1 + e * \alpha \pmod{q};
computing s2 = \beta 2 + e * k \pmod{q}; and
outputting the triple (r, sl, s2) as the proof c.
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10. The method of claim 2 wherein the encrypted message is decrypted by a recipient using the steps of:

computing $B = b^{x_d} \pmod{p}$, where x_d is a secret key corresponding to a public key

computing $K = hash(a/B \mod p)$; and computing the message M as $M = D_K(M')$.

- 11. The method of claim 8 wherein the proof of correctness comprising the proof c in the form of the triple (r, sl, s2) is checked by computing e = hash(r, a) and verifying that $y_d^{sl} * g^{s2} = r *$ a^e .
- 12. The method of claim 1 wherein if the check of the proof of correctness indicates that the proof is invalid, the module of the server directs that the encrypted message be discarded.

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 y_d ;

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- 13. The method of claim 1 wherein the network comprises a plurality of servers, and wherein each of at least a subset of the servers includes a module for checking the proof of correctness if the corresponding encrypted message passes through the corresponding server in being transmitted from a sender to the recipient through the network.
- 14. The method of claim 1 wherein the one or more escrow authorities comprises an escrow authority associated with a public key used for encryption of the message, and wherein the escrow authority associated with the public key is able to decrypt the encrypted message to obtain a plaintext message.
- 15. The method of claim 14 wherein the escrow agent associated with the public key is able to decrypt the encrypted message without exposing a corresponding secret key, using a threshold-based method.
- 16. The method of claim 1 wherein associated with the encrypted message is a first element that is generated using a public key of the recipient and can be decrypted by a party holding the corresponding secret key, and a second element that proves that the first element can be decrypted by a party holding the corresponding secret key.
- 17. An apparatus for encrypting a message to be transmitted over a network, wherein the apparatus comprises:
- a processor-based device for encrypting the message for transmission over the network, the resulting encrypted message having associated therewith a proof of correctness indicating that the message is of a type that allows decryption by one or more escrow authorities; wherein the encrypted message is transmitted through the network to a recipient, and in traversing the network the proof of correctness associated with the encrypted message is checked by at least one module of a server of the network.

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- 18. An article of manufacture comprising one or more software programs for use in encrypting a message to be transmitted over a network, wherein the one or more software programs when executed implement the step of:
- encrypting the message for transmission over the network, the resulting encrypted message having associated therewith a proof of correctness indicating that the message is of a type that allows decryption by one or more escrow authorities;

wherein the encrypted message is transmitted through the network to a recipient, and wherein in traversing the network the proof of correctness associated with the encrypted message is checked by at least one module of a server of the network.